

SUB-OPTIMAL CONTROL OF SINGLE-SPOOL JET ENGINE USING REAL-TIME MODEL

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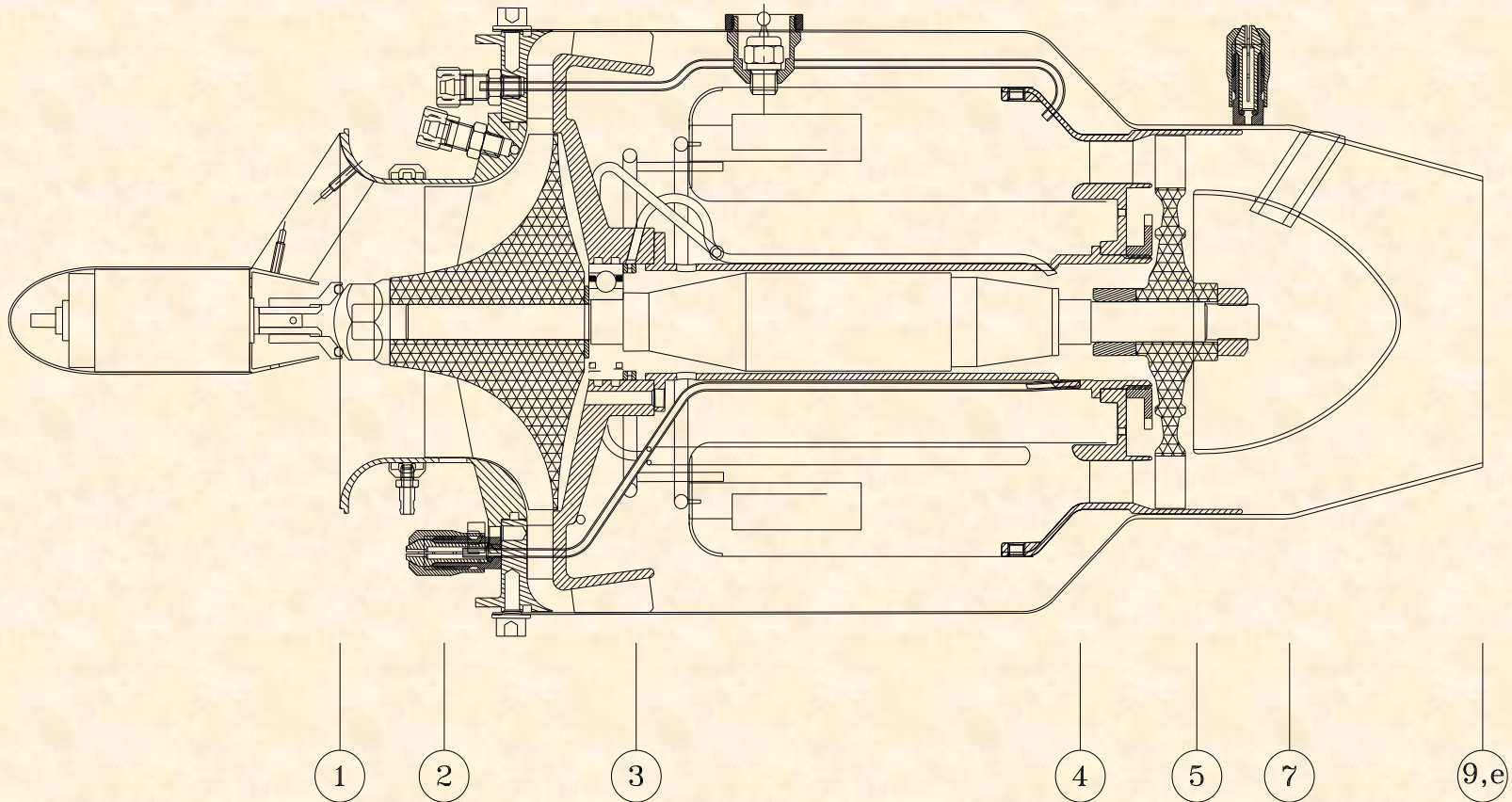
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Objectives:

- Development of a sub-optimal minimum-time controller for single - spool jet engine
- Development of algorithm for engine control based on back-up for faulty sensors

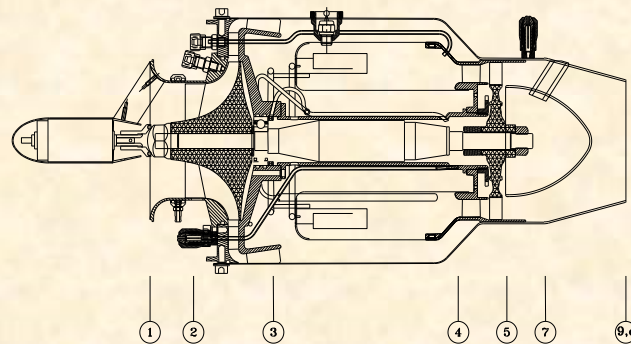
Engine Stations



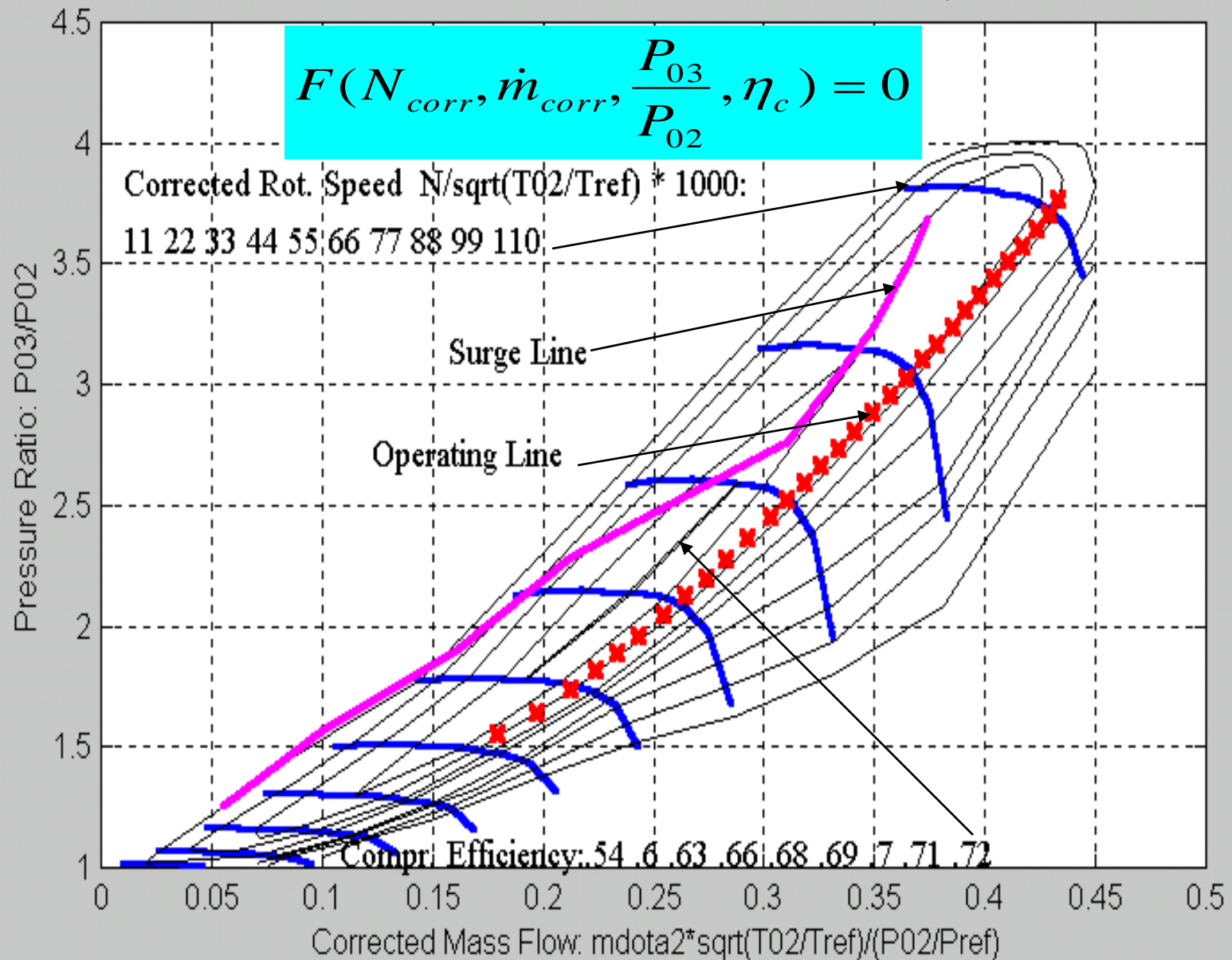
Conventional Nonlinear Engine Model

$$F_D\left[\frac{dx}{dt}, x, y, u, A(x, y, u)\right] = 0$$

$$F_A[x, y, u, B(x, y, u)] = 0$$



"MICROJET" COMPRESSOR MAP. H= 0m; M= 0.



Conventional Nonlinear Engine Model (Continued)

Four Types of Differential Equations

1. The power balance
2. Unsteady flow volume dynamics:
 - a. Continuity
 - b. Energy storage
3. Metal – fluid heat exchange (“heat soakage”)
4. Time delay in the combustion process

1. Power Balance Differential Equation

$$\dot{m}_T \cdot \Delta h_{0,T} \cdot \eta_m - \dot{m}_C \cdot \Delta h_{0,C} - altpower = \frac{dE}{dt}$$

$$E = \frac{J \cdot \left(\frac{N \cdot 2\pi}{60} \right)^2}{2} = \frac{J \cdot N^2 \cdot \pi^2}{1800}$$

$$N = \frac{30}{\pi} \cdot \sqrt{\frac{2E}{J}}$$

2. Unsteady Flow Volume Dynamics

a. Continuity Equation

$$\dot{m}_{out} - \dot{m}_{in} = Vol \cdot \left(1 + \frac{\gamma - 1}{2} * M^2\right)^{\frac{1}{1-\gamma}} \cdot \frac{1}{R \cdot \bar{T}_0} \cdot \left(\frac{d\bar{P}_0}{dt} - \frac{d\bar{T}_0}{dt} \cdot \frac{\bar{P}_0}{\bar{T}_0}\right)$$

b. Energy Storage (Equation of Power for Combustor Chamber)

$$\begin{aligned} \dot{m}_{out} \cdot C_{p,out} \cdot T_{0,out} - \dot{m}_{in} \cdot C_{p,in} \cdot T_{0,in} - \frac{dQ_f}{dt} - \frac{dQ_{soak}}{dt} = \\ (\dot{m}_{out} - \dot{m}_{in} - \dot{m}_f) \cdot \frac{C_v}{1 + \frac{\gamma - 1}{2} \cdot M^2} \cdot \bar{T}_0 + \frac{Vol \cdot C_v}{R} \cdot \frac{1}{\left(1 + \frac{\gamma - 1}{2} \cdot M^2\right)^{\frac{\gamma}{\gamma - 1}}} \cdot \frac{\bar{P}_0}{\bar{T}_0} \cdot \frac{d\bar{T}_0}{dt} \end{aligned}$$

3. Heat Soakage

$$\frac{dQ_{soak}}{dt} = h \cdot A \cdot (\bar{T}_{metal} - \bar{T}_{gas})$$

$$m_{metal} \cdot C_{p,metal} \cdot \frac{d\bar{T}_{metal}}{dt} + h \cdot A \cdot \bar{T}_{metal} = h \cdot A \cdot \bar{T}_{gas}.$$

h - heat transfer coefficient, $\frac{W}{m^2 \cdot K}$

4. Time Delay of the Combustion Process

$$\tau_f \cdot \frac{d\dot{m}_{f,out}(t)}{dt} + \dot{m}_{f,out}(t) = \dot{m}_{f,in}(t - \tau_0)$$

Control System Specifications:

1. Corrected rotational speed control: $(\frac{N}{\sqrt{T_{02}}})$

a) Steady-state error: <1%

b) Settling time: minimum

c) Overshoot: <2%

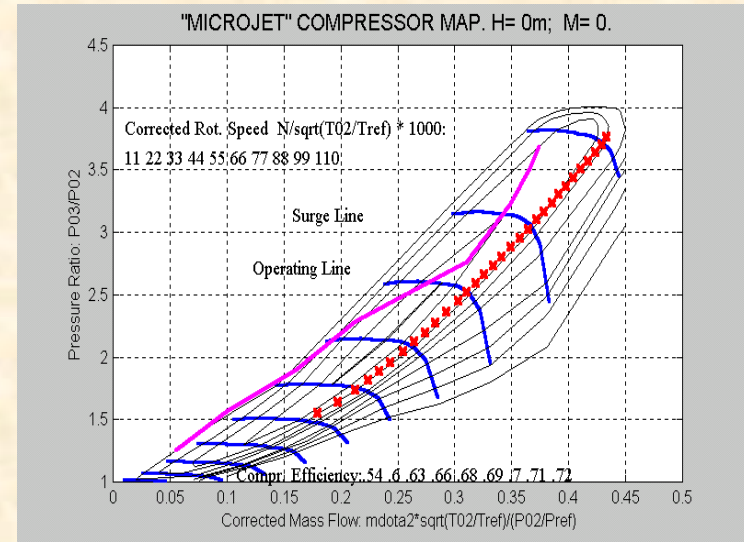
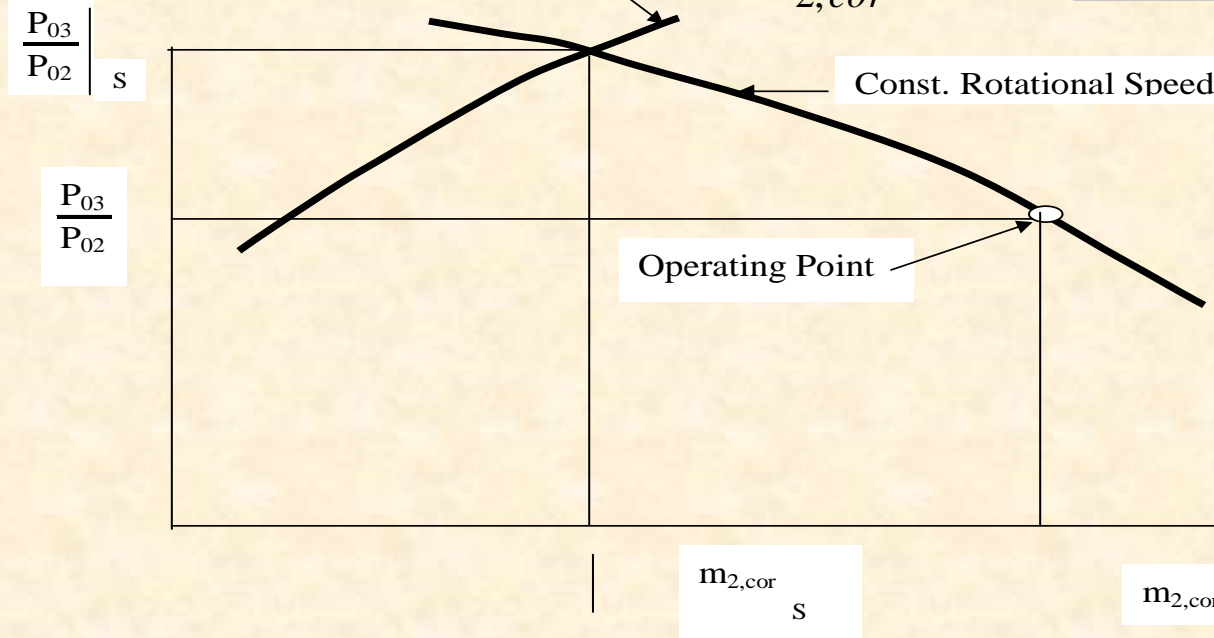
2. $T_{05} < T_{05max}$ (EGT)

3. Equivalence Ratio: $\phi_{min} < \phi < \phi_{max}$

$$\phi = \frac{\frac{\dot{m}_f}{\dot{m}_a}}{\frac{\dot{m}_f}{\dot{m}_a} \big|_{stoichiom}}$$

4. Stall margin: >5%

$$SM = \frac{\left(\frac{P_{03}}{P_{02}}\right)_S - \frac{P_{03}}{P_{02}}}{\frac{(\dot{m}_{2,cor})_S - \dot{m}_{2,cor}}{\frac{P_{03}}{P_{02}}}}$$



Concept of Sub-Optimal Control of a Single-Spool Engine

1. Conventional linearization for the nonlinear engine model is not desirable
2. Sub-optimal control has to provide:
 - a) dynamic operating line close to the surge line during engine acceleration (maximum fuel rate)
 - b) equivalence ratio close to a minimal limiting value during engine deceleration (minimum fuel rate)

Engine Model for Real-Time Simulations

Variable Vectors:

$$u = [\dot{m}_f, H, M]$$

$$x = [N_{corr}, \dot{m}_a, \frac{P_{03}}{P_{02}}, T_{05}, T]$$

$$y = [N_{corr}, \dot{m}_{a,corr}, \frac{P_{03}}{P_{02}}, T_{05}, T, SM, \varphi, ...]$$

$$x_0 = [N_{corr\ 0}, \dot{m}_{a\ 0}, (\frac{P_{03}}{P_{02}})_0, T_{05\ 0}, T_0]$$

Engine Model for Real-Time Simulations (continued)

Differential Equations:

$$\tau_{N_{cor}}(H, M, \Delta N_{cor}) \frac{d(\Delta N_{cor})}{dt} + \Delta N_{cor} = K_{N_{cor}}(H, M, \Delta N_{cor}) \Delta \dot{m}_f$$

$$\tau_{P_{32}}(H, M, \Delta N_{cor}) \frac{d(\Delta P_{32})}{dt} + \Delta P_{32} = K_{P_{32}}(H, M, \Delta N_{cor}) \Delta \dot{m}_f$$

$$\tau_T(H, M, \Delta N_{cor}) \frac{d(\Delta T)}{dt} + \Delta T = K_T(H, M, \Delta N_{cor}) \Delta \dot{m}_f$$

$$\tau_{2, \dot{m}_a}(H, M, \Delta N_{cor}) \frac{d(\Delta \dot{m}_a)}{dt} + \Delta \dot{m}_a = K_{\dot{m}_a}(H, M, \Delta N_{cor}) (\tau_{1, \dot{m}_a}(H, M, \Delta N_{cor}) \frac{d(\Delta \dot{m}_f)}{dt} + \Delta \dot{m}_f)$$

$$\tau_{2, T_{05}}(H, M, \Delta N_{cor}) \frac{d(\Delta T_{05})}{dt} + \Delta T_{05} = K_{T_{05}}(H, M, \Delta N_{cor}) (\tau_{1, T_{05}}(H, M, \Delta N_{cor}) \frac{d(\Delta \dot{m}_f)}{dt} + \Delta \dot{m}_f)$$

Engine Model for Real-Time Simulations (continued)

Algebraic Equations:

$$\dot{m}_f = \dot{m}_{f0} + \Delta \dot{m}_f$$

$$N_{cor} = N_{cor0} + \Delta N_{cor}$$

$$P_{32} = P_{320} + \Delta P_{32}$$

$$T = T_0 + \Delta T$$

$$\dot{m}_a = \dot{m}_{a0} + \Delta \dot{m}_a$$

$$T_{05} = T_{050} + \Delta T_{05}$$

$$\left(\frac{P_{02}}{P_a} \right) = \left[1 + \eta_d \frac{\gamma_a - 1}{2} M^2 \right]^{\frac{\gamma_a}{\gamma_a - 1}}$$

$$\left(\frac{T_{02}}{T_a} \right) = 1 + \frac{\gamma_a - 1}{2} M^2$$

Engine Model for Real-Time Simulations (continued)

Algebraic Equations:

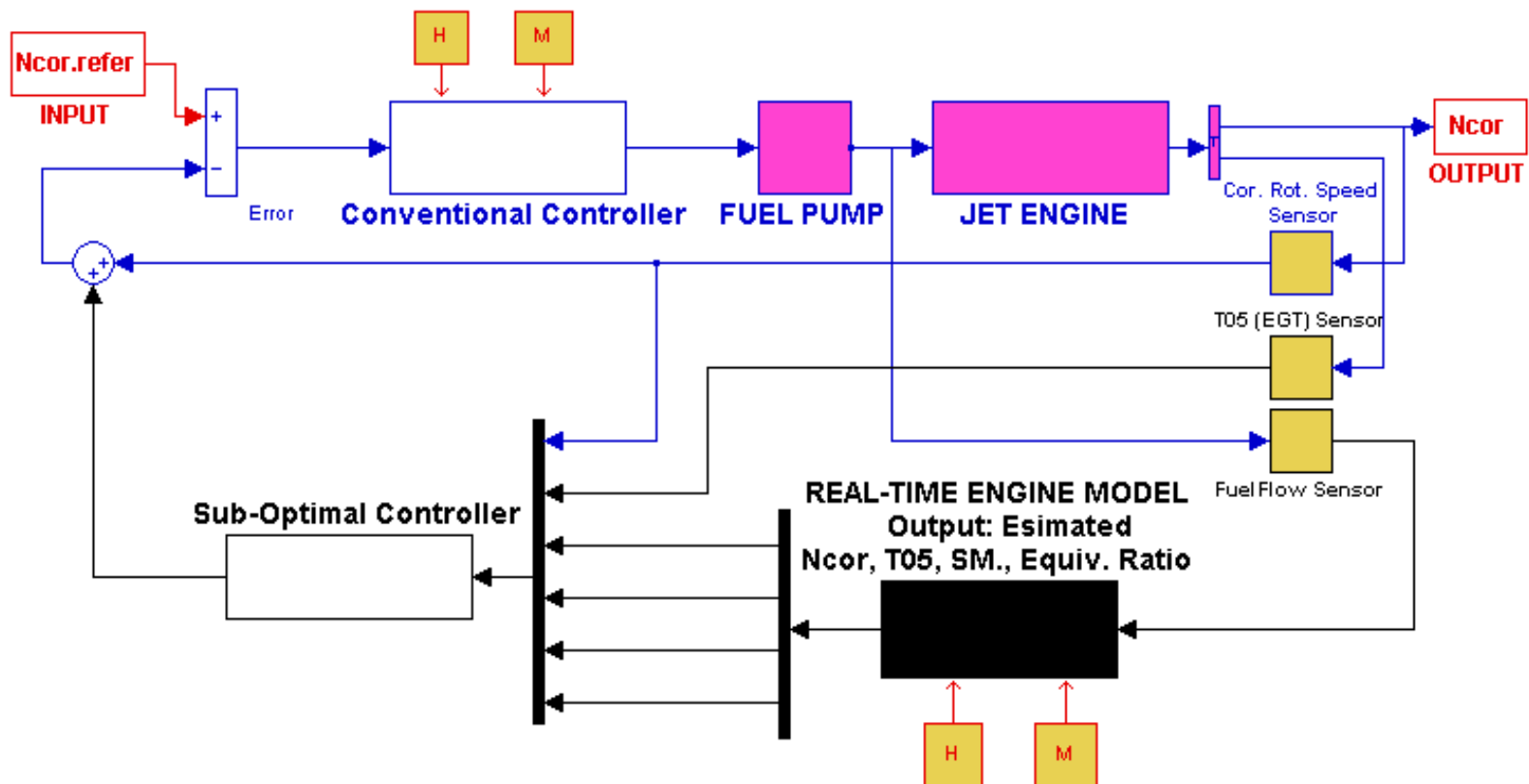
$$\dot{m}_{2a_{cor}} = \frac{\dot{m}_a \cdot (1 + \varepsilon) \cdot \sqrt{\frac{T_{02}}{T_{ref}}}}{\frac{P_{02}}{P_{ref}}}$$

$$SM = \frac{\frac{(P_{32})_{stall}}{(\dot{m}_{2a_{cor}})_{stall}} - \frac{P_{32}}{\dot{m}_{2a_{cor}}}}{\frac{P_{32}}{\dot{m}_{2a_{cor}}}}$$

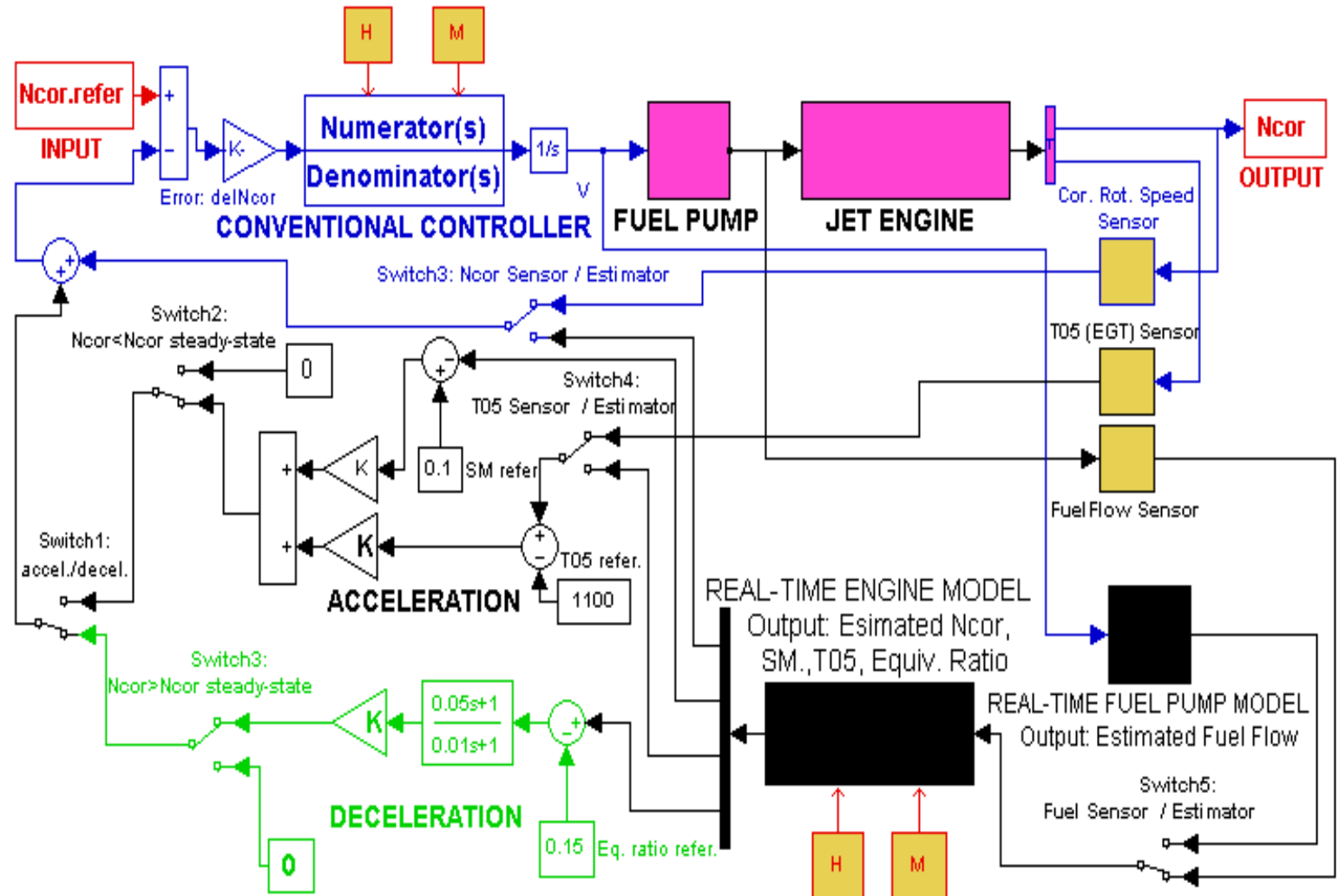
$$\phi = \frac{\frac{\dot{m}_f}{\dot{m}_a}}{\frac{\dot{m}_f}{\dot{m}_a} \big|_{stoichiom}}$$

$$Note : P_{32} = \frac{P_{03}}{P_{02}}$$

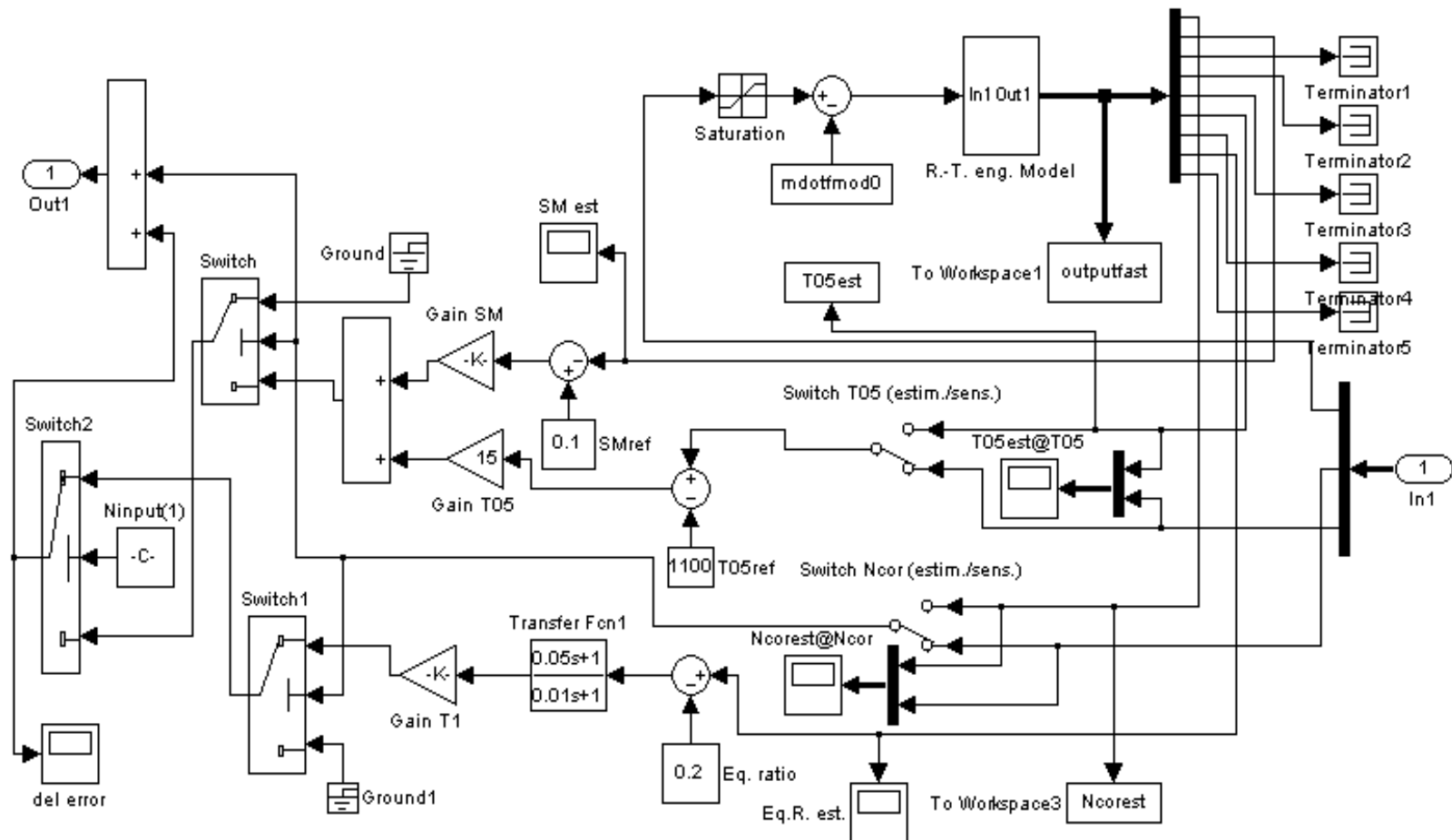
Block-Diagram of Sub-Optimal Engine Control System



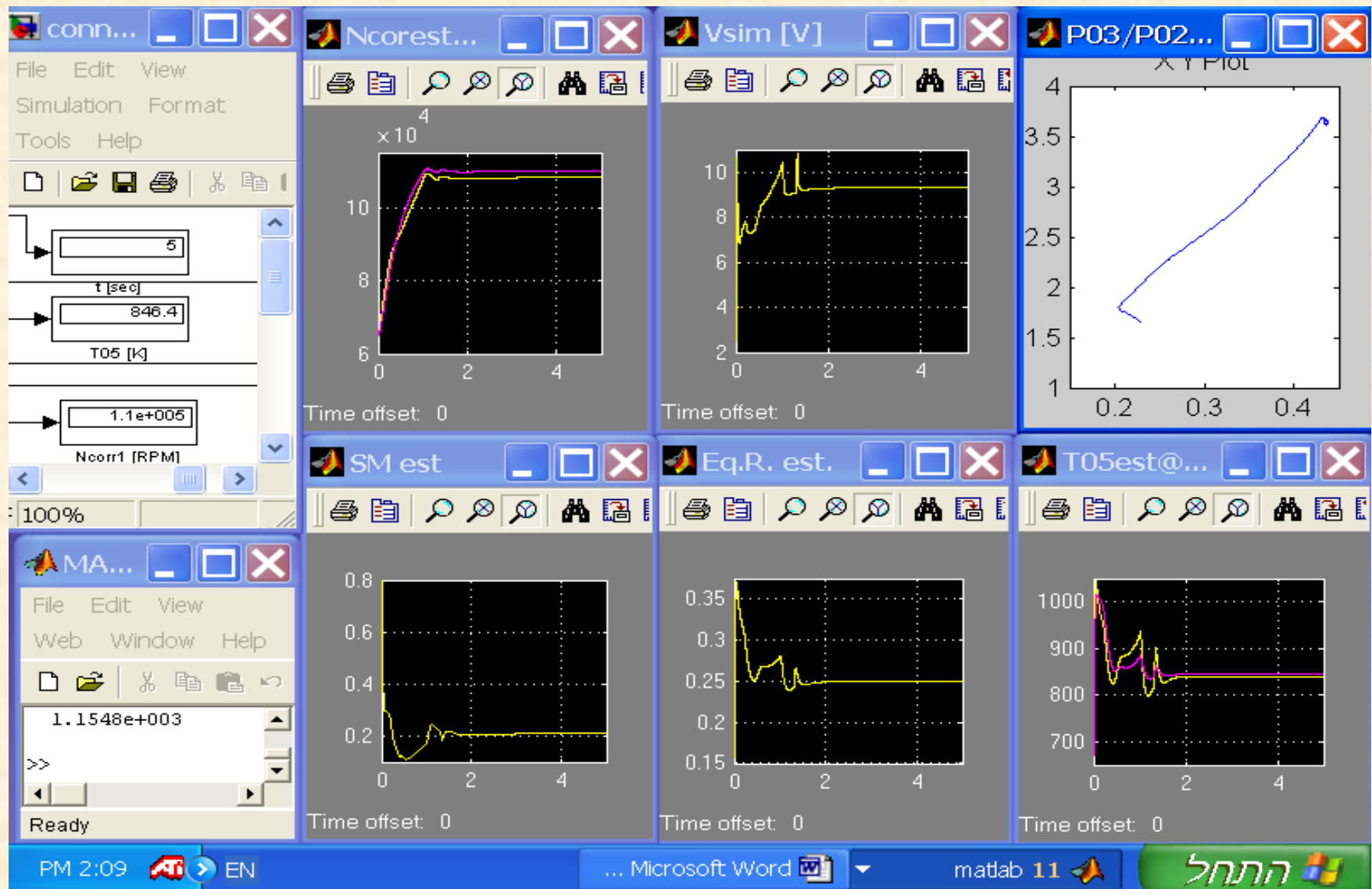
Sub-Optimal Controller



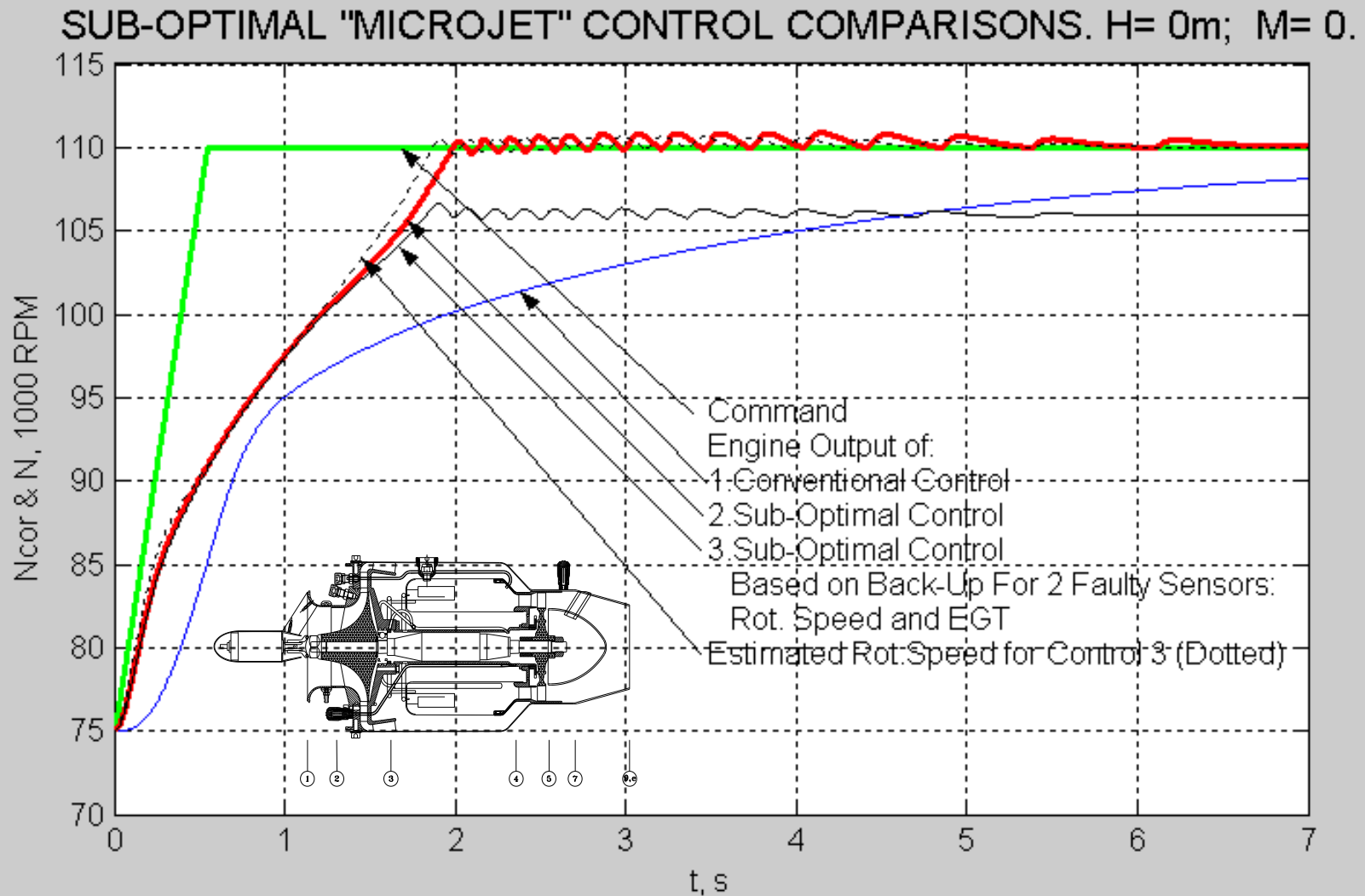
Simulink Code of Sub-Optimal Engine Controller



Screen View During Simulations of Sub-Optimal Control

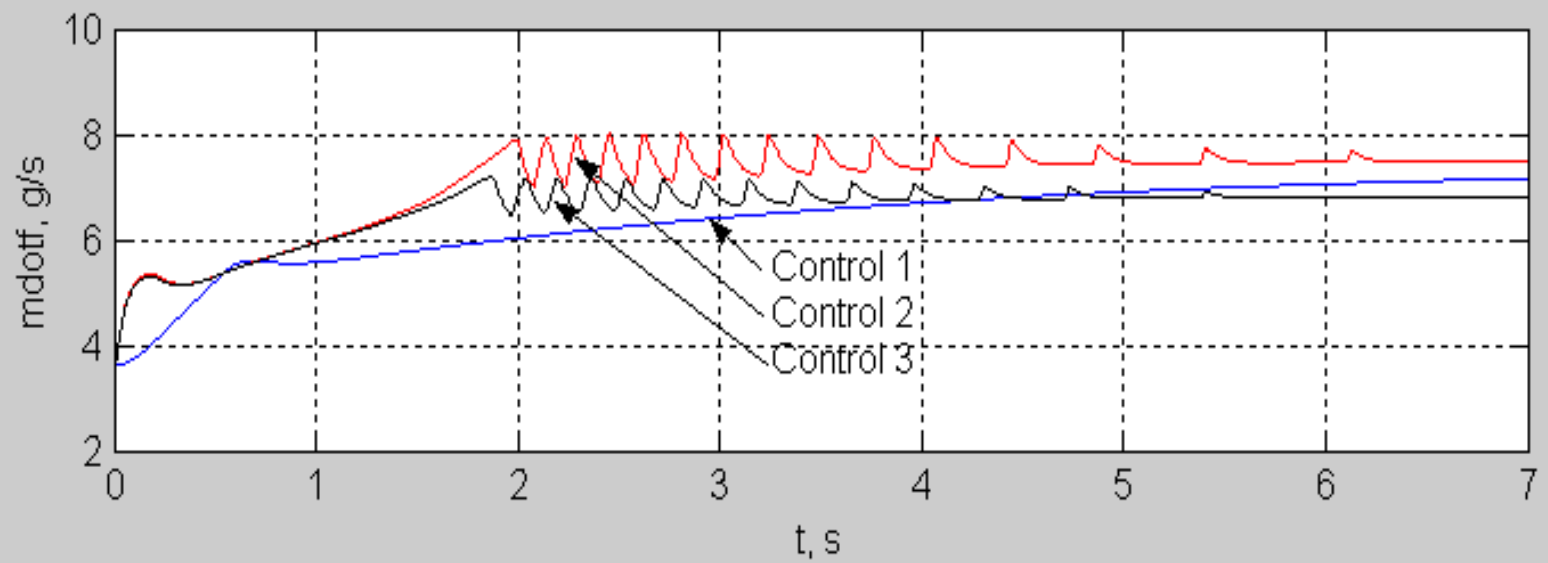
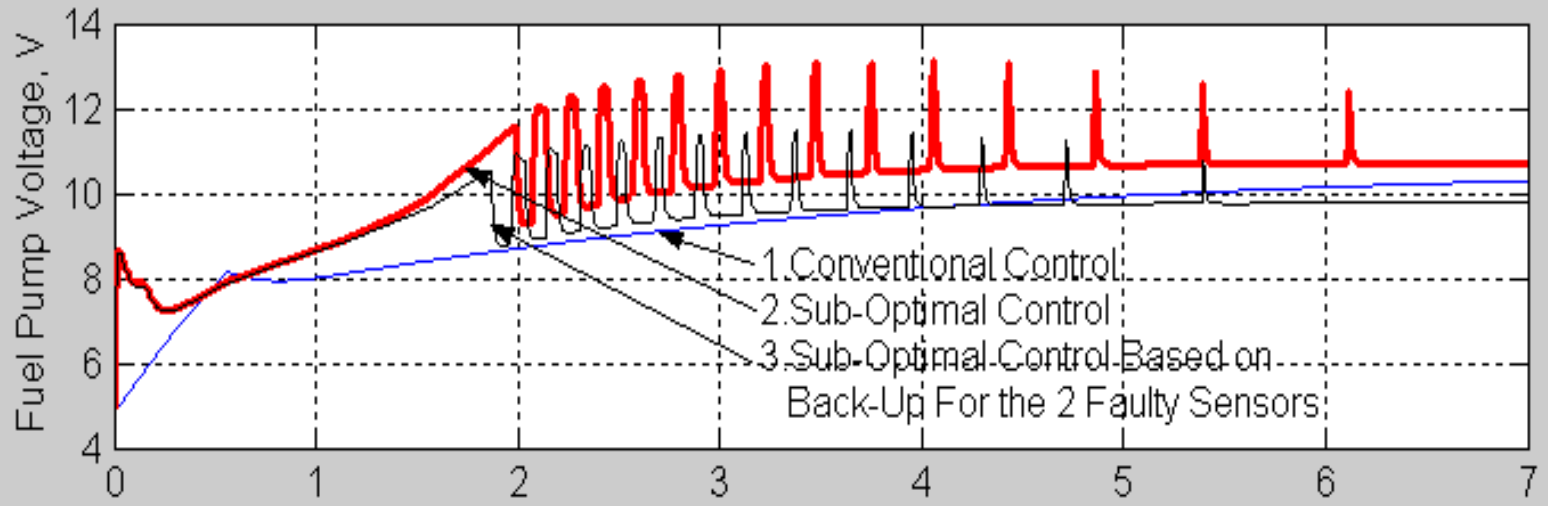


Corrected Rotational Speed During Engine Acceleration



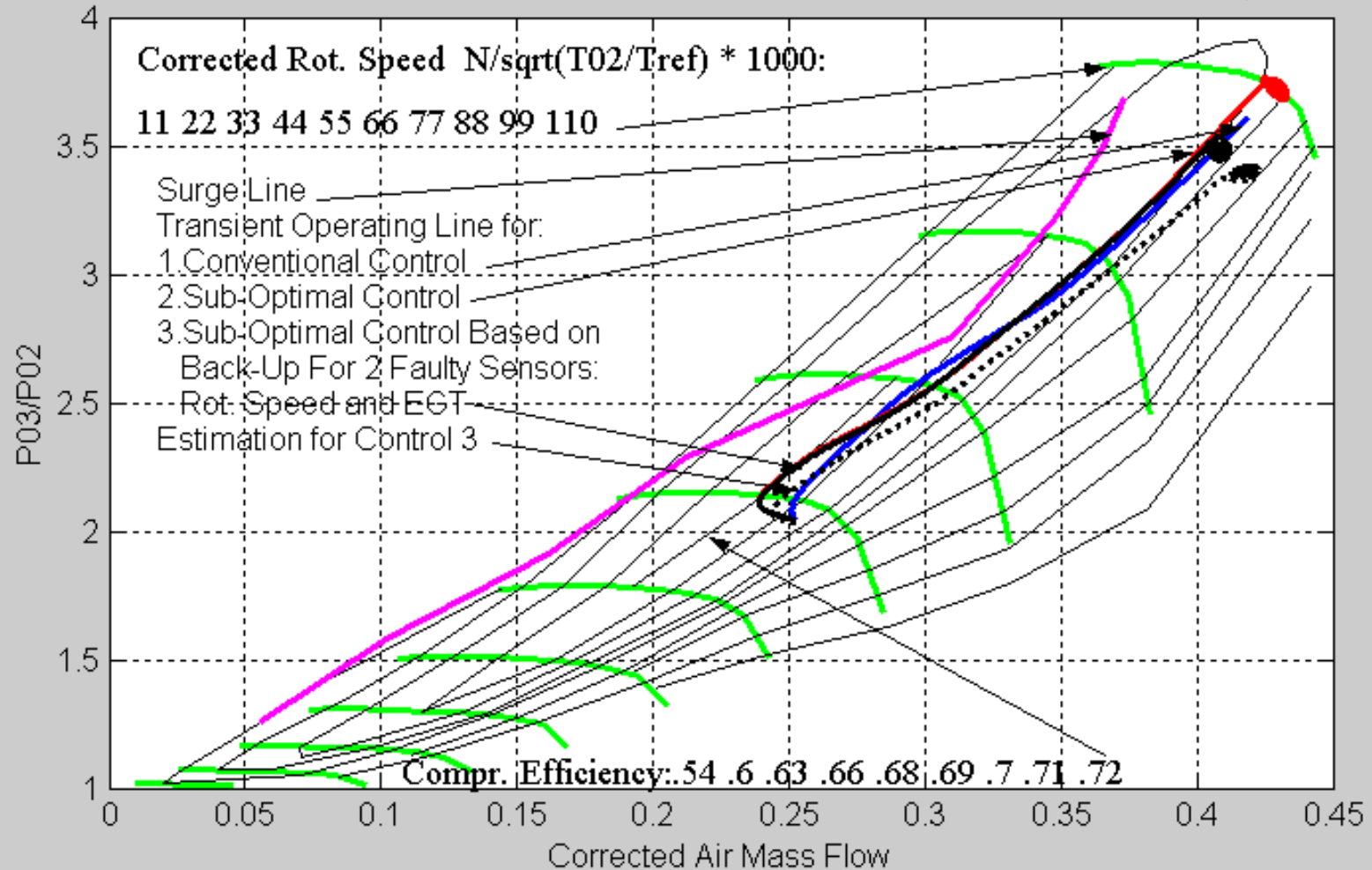
Fuel Pump Voltage and Fuel Mass Flow During Engine Acceleration

SUB-OPTIMAL "MICROJET" CONTROL COMPARISONS. H= 0m; M= 0.

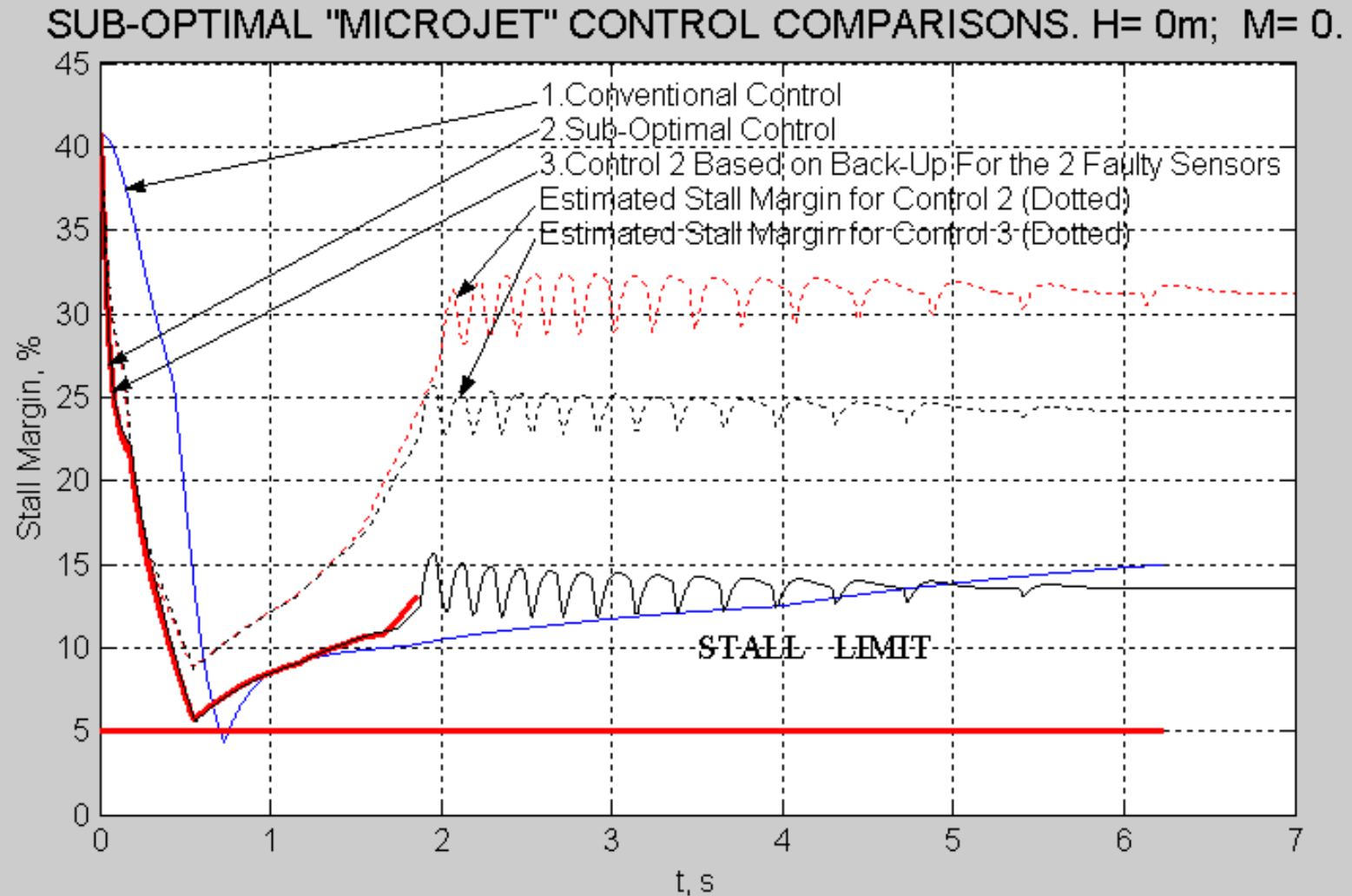


Transient Operating Line During Engine Acceleration

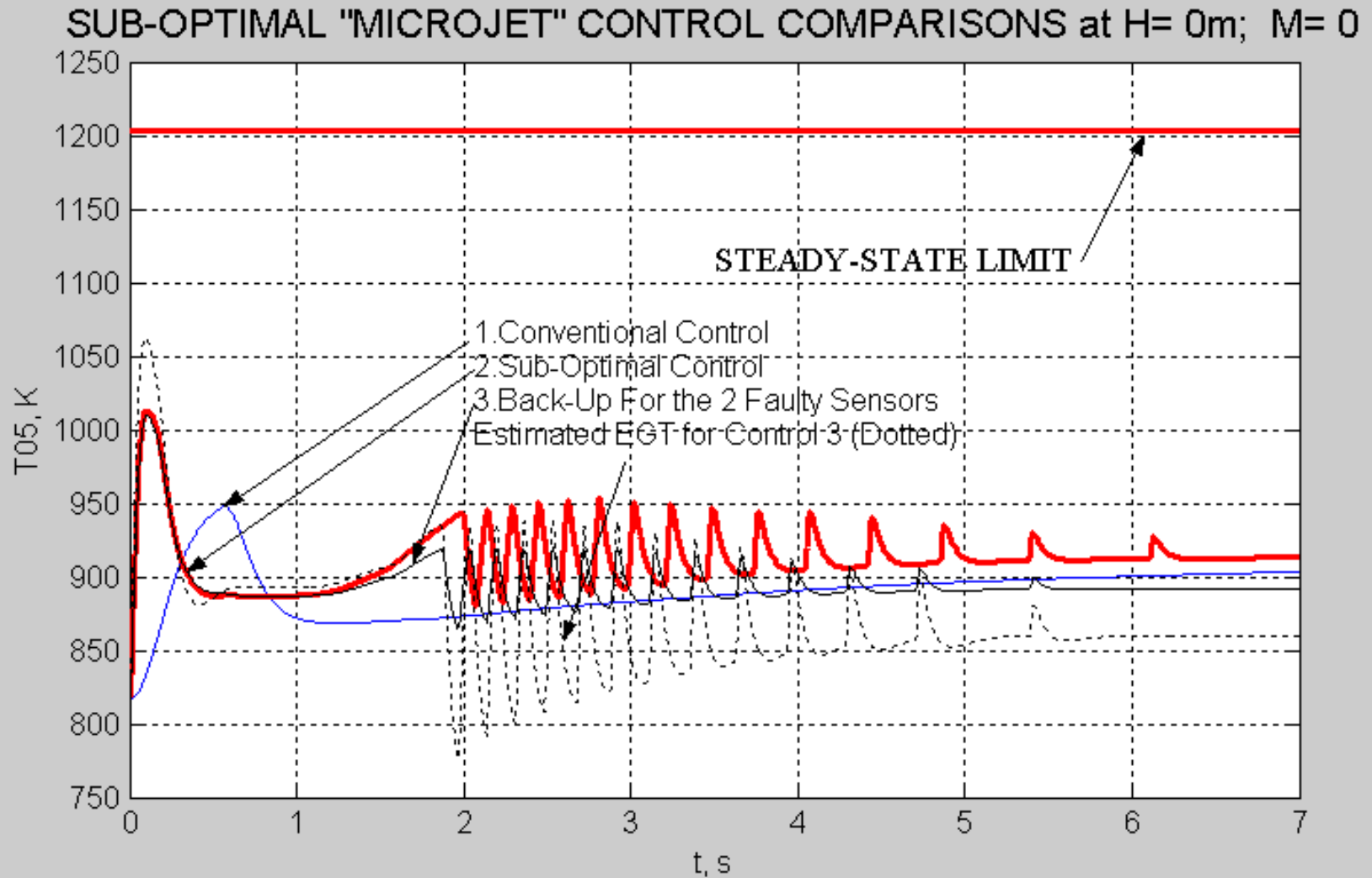
SUB-OPTIMAL "MICROJET" CONTROL COMPARISONS. H= 0m; M= 0.



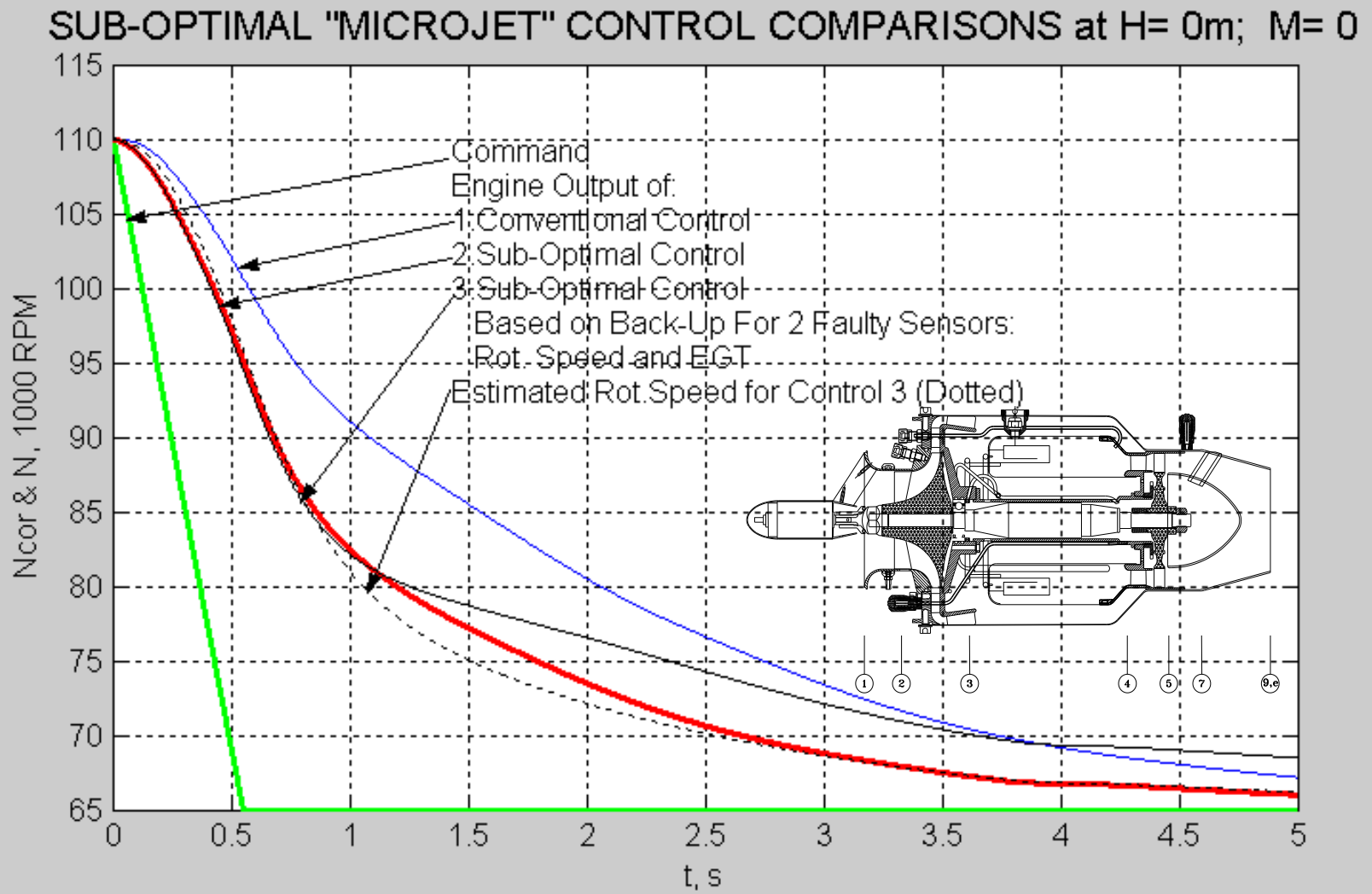
Stall Margin During Engine Acceleration



Output Turbine Temperature (EGT)

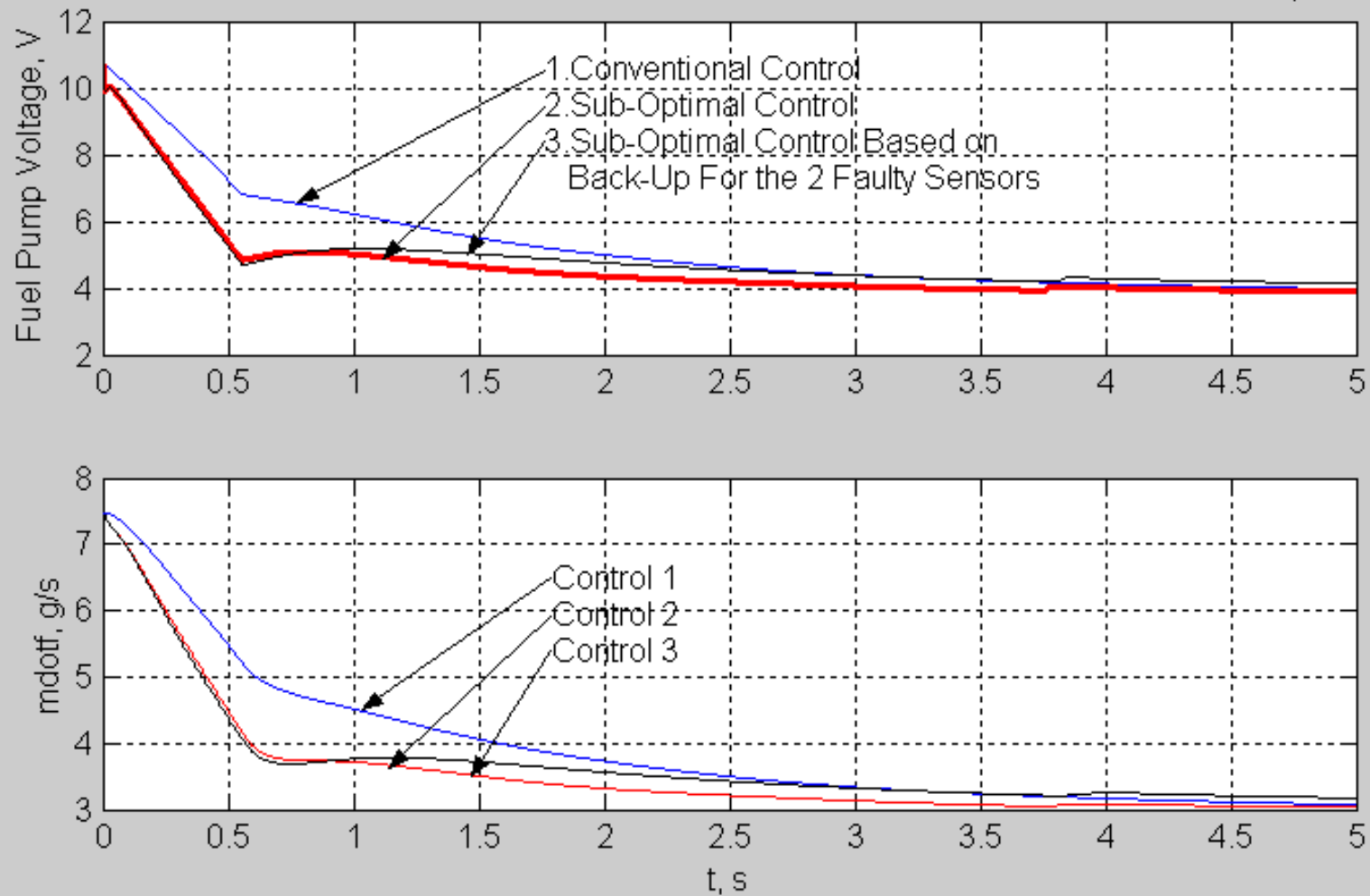


Corrected Rotational Speed During Engine Deceleration

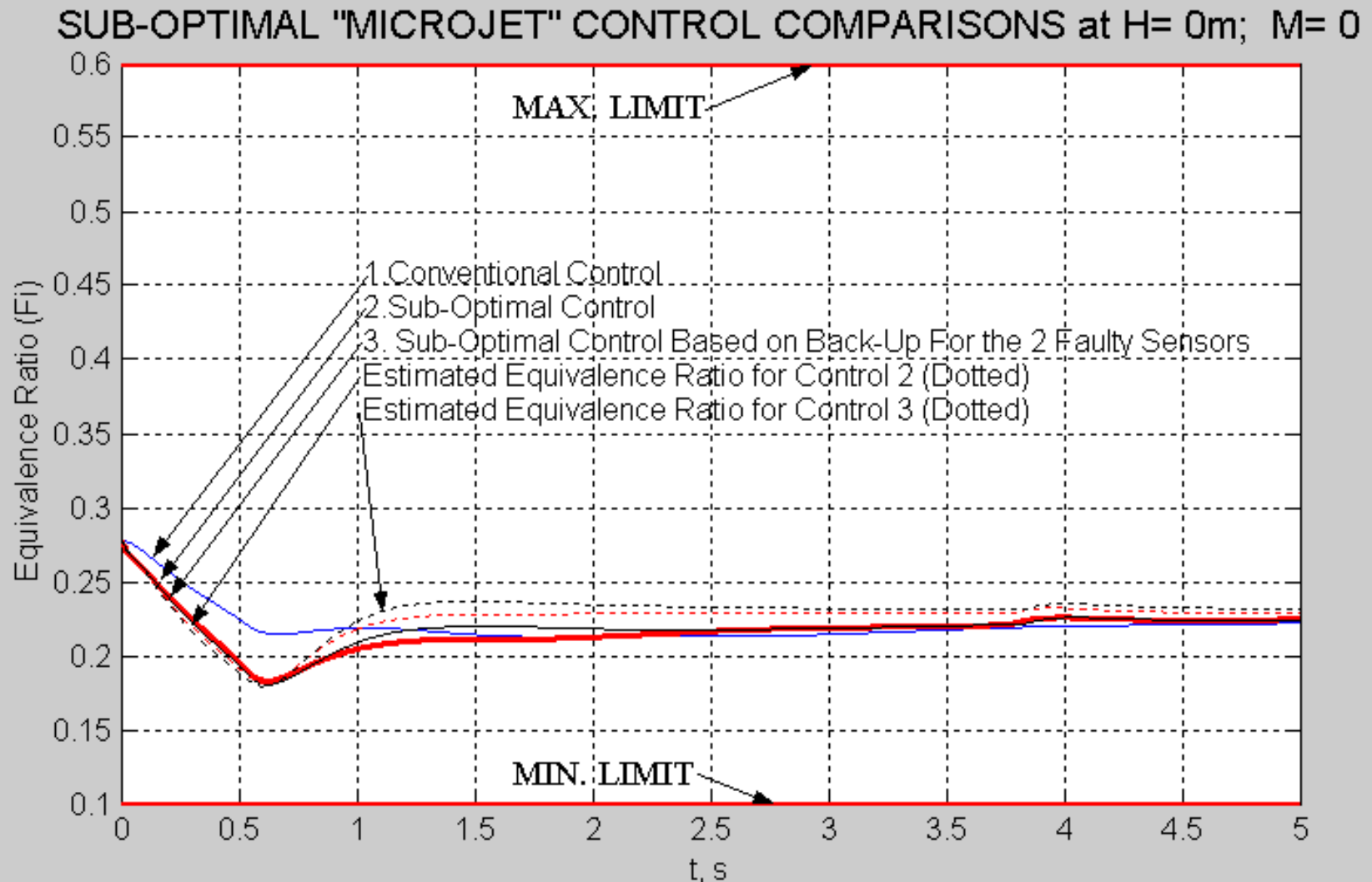


Fuel Pump Voltage and Fuel Mass Flow

SUB-OPTIMAL "MICROJET" CONTROL COMPARISONS at $H=0\text{m}$; $M=0$



Equivalence Ratio During Engine Deceleration



CONCLUSIONS

- Conventional linearization for the nonlinear engine model is not desirable
- Sub-optimal control provides:
 - a) dynamic operating line close to the surge line during engine acceleration (maximum fuel rate)
 - b) equivalence ratio close to a minimal limiting value during engine deceleration (minimum fuel rate)
- The fast engine model may be used on-line, both, for unmeasured parameter estimations and as a back-up for faulty sensors

THE END